

DIGITAL TECHNICS

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5b. LECTURE: SEQUENTIAL CIRCUITS BASICS AND FLIP-FLOPS



1st (Autumn) term 2018/2019

5. LECTURE

1. Sequential logic, basic principles
2. Synchronous and asynchronous logic circuits
3. Flip-flops

SEQUENTIAL LOGIC CIRCUITS

The combinational logic circuits have no memory. The outputs always follow the inputs.

There is an other group of circuits with a memory, which behave differently *depending upon their previous state*.

An example is the vending machine, which must remember how many and what kinds of coins have been inserted, and which behave according to not only the current coin inserted, but also upon how many and what kind of coins have been deposited previously in the given service cycle. In fact its response depends on the whole sequence of previous events.

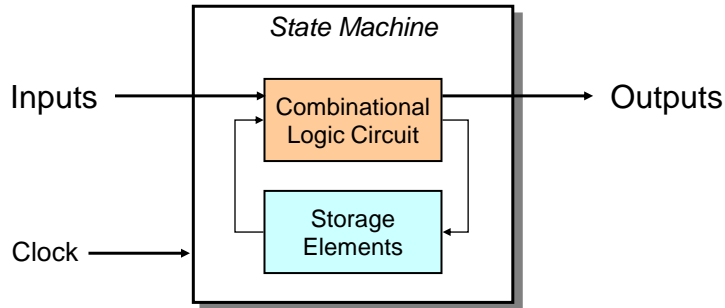
These are referred to as *sequential circuits* or *finite state machines*, because they can have at most a finite number of states.

FINITE STATE MACHINE

- A description of a system with the following components:
 1. A finite number of **states**
 2. A finite number of external **inputs**
 3. A finite number of external **outputs**
 4. An explicit specification of all **state transitions**
 5. An explicit specification of what determines each external **output value**
- Often described by a state diagram.
 - Inputs trigger state transitions.
 - Outputs are associated with each state (or with each transition).

IMPLEMENTING A FINITE STATE MACHINE

- **Combinational logic**
 - Determine outputs and next state.
- **Storage elements**
 - Maintain state representation.



INTRODUCTORY EXAMPLE: VENDING MACHINE

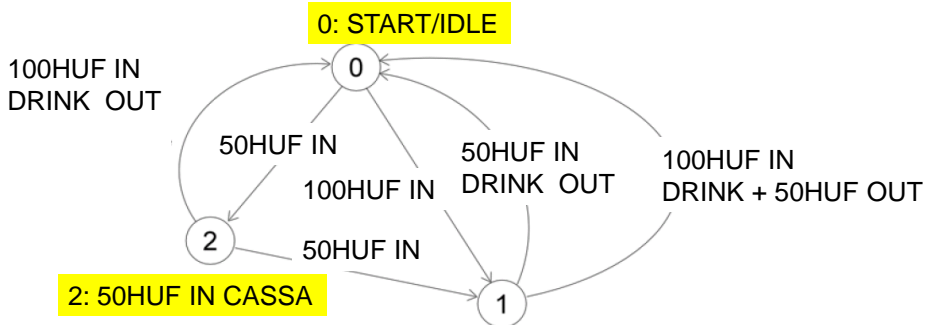
E.g. consider a bottled drink vending machine which vends a bottled drink costing 150 HUF, and accepts coins of 50 HUF and 100 HUF. It should "remember" how many and what kind of coins have already been inserted into it.

The "response" of the machine depends not only on the coin last inserted, but also on how many and what kind of coins it accepted already in the given service cycle.

It should serve the bottle, and change if appropriate, when a number of coins with a total value of 150 HUF or more have been inserted into the slot.

In fact its response depends on the whole sequence of previous events.

DESCRIPTION OF STATES OF A DRINK VENDING MACHINE

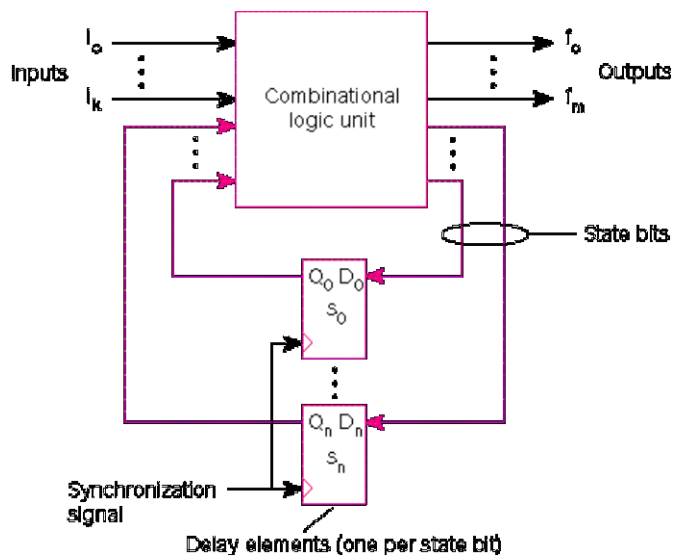


Drink: 150 Ft
Coin: 50 or 100 Ft

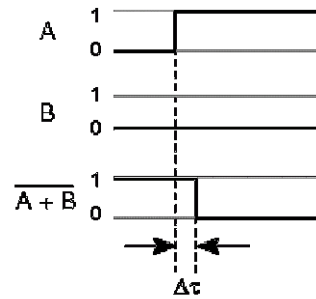
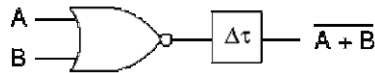
Number of states: 3 (START/IDLE, 50HUF IN CASSA, 100HUF IN CASSA)

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FINITE STATE MACHINE: CLASSICAL MODEL



A NOR GATE WITH A LUMPED DELAY

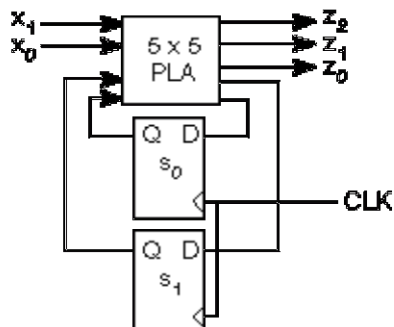


Timing behavior

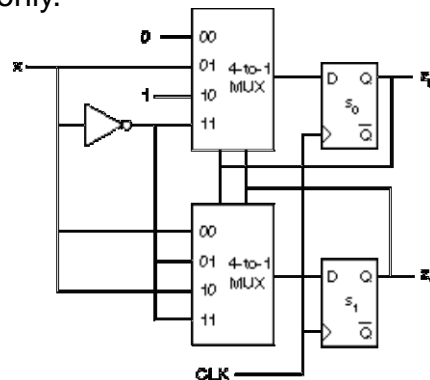
This delay between input and output is at the basis of the functioning of an important memory (storage) element, the *flip-flop*.

MEALY VERSUS MOORE MACHINES

Mealy Model: Outputs are functions of Inputs and present state.



Moore Model: Outputs are functions of present state only.



Both are equally powerful.

MULTIVIBRATORS AND FLIP-FLOPS

Multivibrators, like the familiar sinusoidal oscillators, are circuits with regenerative feedback, with the difference that they produce pulsed output. There are three basic types of multivibrator, namely the bistable multivibrator, the monostable multivibrator and the astable multivibrator.

Flip-flop, latch or bistable multivibrator

is an electronic circuit which has two stable states. It is capable to function as a memory.

A flip-flop is controlled by one or two control signals and/or a gate or clock signal. The output often includes the complement as well as the normal output.

Sometimes they have separate auxiliary clear and load/set/preset inputs too.

FLIP-FLOPS: ELECTRONICS

Flip-flops are circuits that can be found in two stable balanced states (circuit values i.e. voltages, currents) do not change. Stable either permanently (change only due to an external pulse) or temporarily (after a certain time change into other state spontaneously).

The circuit state when the voltages are changing is called non-stable.

Flip-flops can be divided into the following groups, according to the character of the stable balanced states:

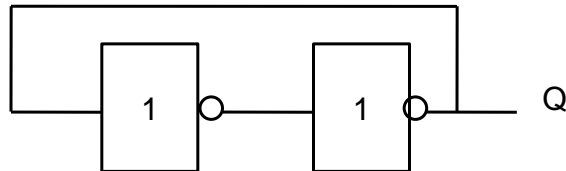
bistable (both states are permanently stable),

monostable (often called one-shots) (one of the states is permanently stable, the other one is stable only temporarily),

astable (both states are temporarily stable).

FLIP-FLOPS: ELECTRONICS

The basis for the flip-flops is an amplifier with a positive feedback (pair of simple transistor amplifying stages, or one amplifying stage and a transformer for creating the positive feedback, etc.).

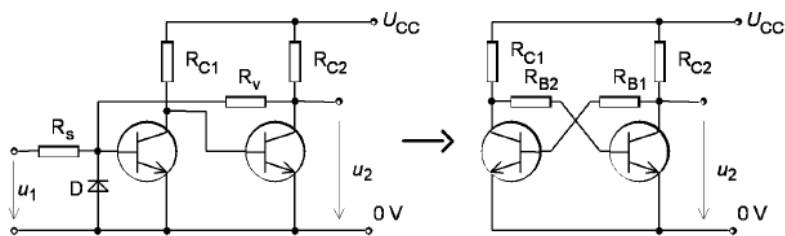


In digital technique a pair of inverters or logical elements with similar behaviour are often used.

This circuit can have two stable states, either $Q = 0$ or $Q = 1$

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FLIP-FLOPS: ELECTRONICS

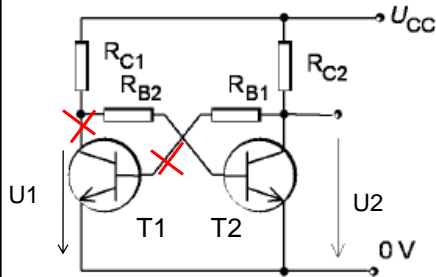


Construction of a bistable flip-flop from two-transistor amplifying stages.

In practice, flip-flops made of discrete transistors are rarely used today.

Being constructed on the basis of different types of integrated circuits, such as timer 555 (integrated circuit most commonly used for this purpose).

FLIP-FLOP: CIRCUIT ANALYSIS



T1 not conducting, T2 saturation

$$U_1 = U_{CC} - I_{B2} R_{C1}$$

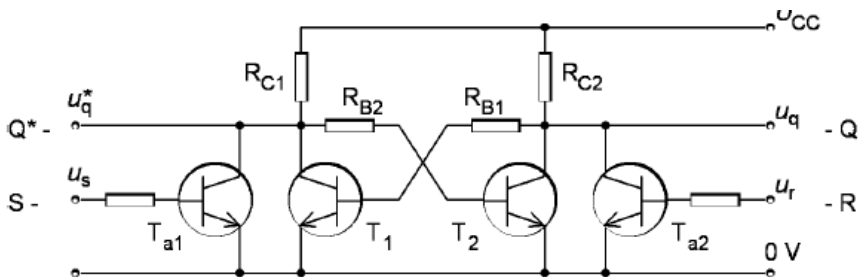
$$U_2 = U_{CEsat}$$

$$I_{B2} = (U_{CC} - U_{BEopen}) / (R_{C1} + R_{B2})$$

$$I_{C2} = (U_{CC} - U_{CEsat}) / R_{C2}$$

Necessary condition: $B I_{B2} > I_{C2} \Rightarrow B > R_{B2} / R_{C2}$

FLIP-FLOPS: ELECTRONICS



Bistable flip-flop with driving transistors (setting/resetting inputs). This is the classical circuit with transistor amplifying stages T1, T2, with driving transistors Ta1, Ta2.

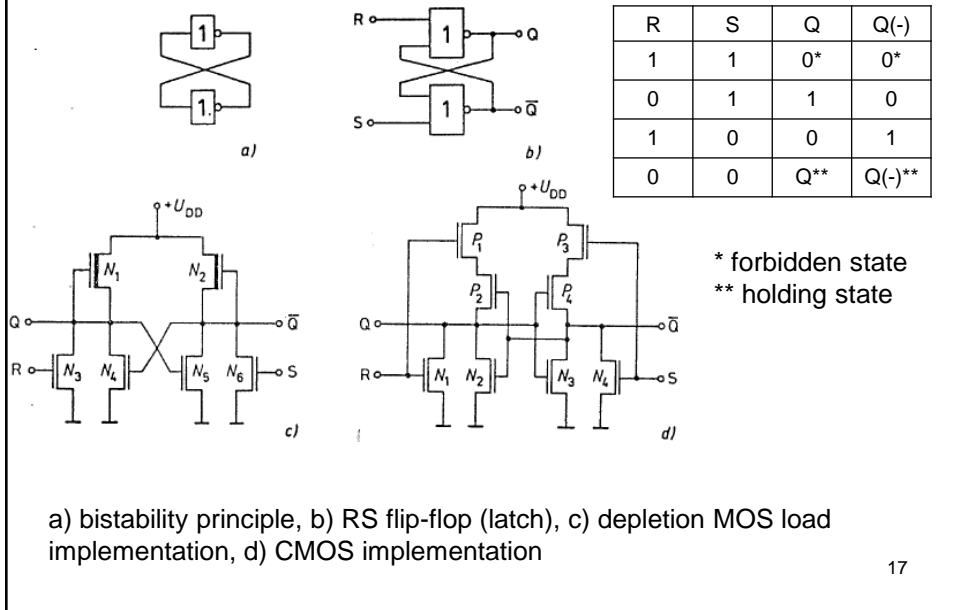
The circuit has two outputs (main, U_q , complementary, U_r) and two driving inputs (setting and resetting).

If $U_s > \sim 0.65 \text{ V}$ Ta1 is switched (saturating), T2 is blocked (cut-off), T1 is switched, Ta2 is blocked, $U_q \approx U_{CC}$.

MOS version: six-transistor SRAM cell.

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BASIC MOS FLIP-FLOP'S (RS)



FLIP-FLOPS

The most important flip-flops types are listed here:

R-S (or S-R) flip-flop	set/reset
J-K flip-flop	set/reset/toggle
T flip-flop	toggle
D flip-flop	data/delay
D-G flip-flop	

All flip-flops listed above can function in **synchronous** or clocked mode, the **R-S** and **D** flip-flops can operate in **asynchronous** mode too.

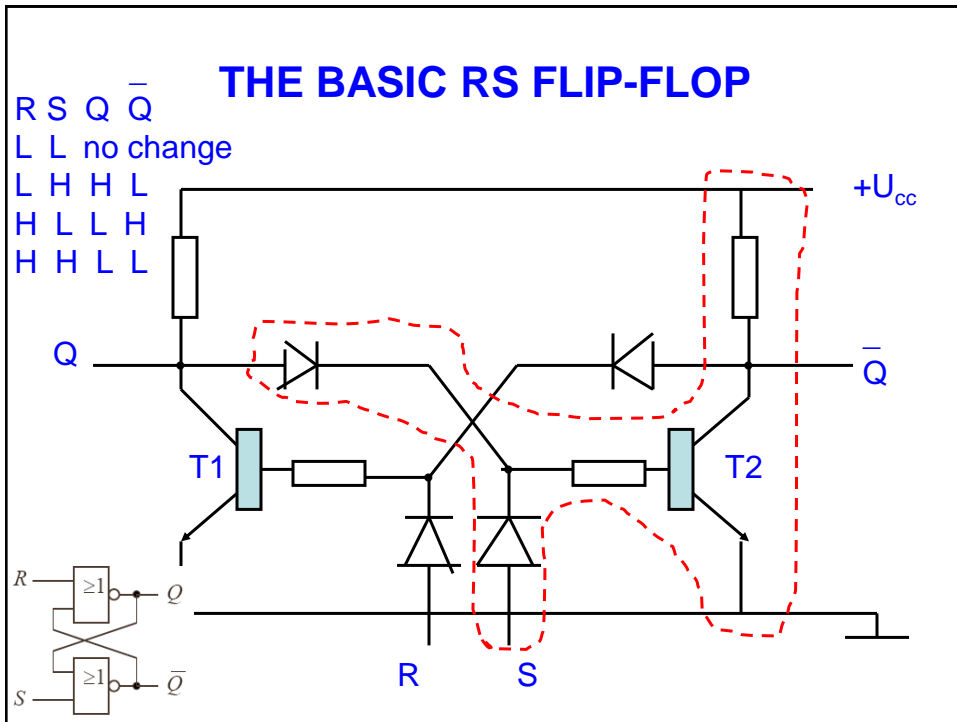
The behaviour of a particular type can be described by truth/characteristic table and the characteristic equation, which gives the next output in terms of the input control signals and the current output.

SUMMARY OF FLIP-FLOP TYPES

FLIP-FLOP NAME	FLIP-FLOP SYMBOL	CHARACTERISTIC TABLE	CHARACTERISTIC EQUATION	EXCITATION TABLE																																			
SR		<table border="1"> <thead> <tr> <th>S</th> <th>R</th> <th>Q_{next}</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>Q</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>?</td> </tr> </tbody> </table>	S	R	Q_{next}	0	0	Q	0	1	0	1	0	1	1	1	?	$Q_{next} = S + R'Q$ $SR = 0$	<table border="1"> <thead> <tr> <th>Q</th> <th>Q_{next}</th> <th>S</th> <th>R</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> <td>X</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>X</td> <td>0</td> </tr> </tbody> </table>	Q	Q_{next}	S	R	0	0	0	X	0	1	1	0	1	0	0	1	1	1	X	0
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STATE TRANSITION DIAGRAMS

NAME	STATE DIAGRAM
SR	
JK	
D	
T	



THE SR FLIP-FLOP OR LATCH

The SR (set/reset) flip-flop is one of the simplest flip/flops used in digital systems. Really it's the most basic of all flip-flops. It can be realized/implemented by direct feedback of a combinational circuit, i.e. with asynchronous sequential circuit.

Characteristic equation (derived from the truth/characteristic table):

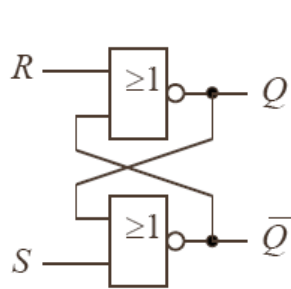
$$Q^{n+1} = S + \bar{R} Q^n = \bar{R} (S + Q^n)$$

and

$$RS = 0$$

Note: in some places it is referred to as SET/CLEAR flip-flop.

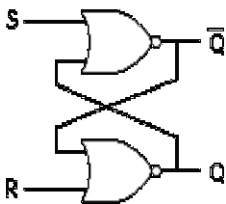
THE SET-RESET FLIP-FLOP



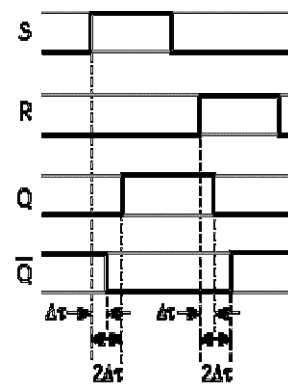
R	S	Q	\bar{Q}	
L	L	no change		
L	H	H	L	
H	L	L	H	
H	H	L	L	undefined!

NOR gates are controlled by HIGH levels on the input!

THE S-R (SET-RESET) FLIP-FLOP: TIMING BEHAVIOUR



Q_t	S_t	R_t	Q_{t+1}
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	(disallowed)
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	(disallowed)



Timing behavior

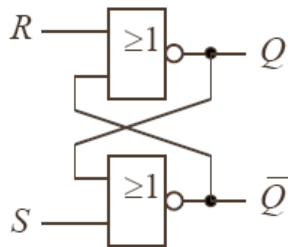
The S-R flip-flop is an active high (positive logic) device.

RS FLIP-FLOP: IMPLEMENTATION WITH NOR GATES

$$Q = R + \bar{Q}$$

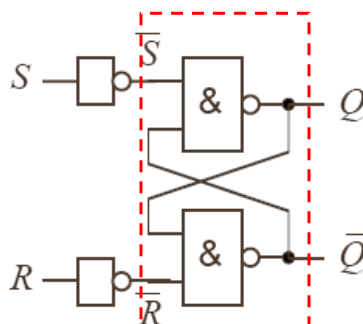
$$\bar{Q} = S + Q$$

Q is the output of the R gate !



S	R	Q	Q̄
0	0	Q ₋₁	Q̄ ₋₁
0	1	0	1
1	0	1	0
1	1	(0)	(0) (not allowed)

RS FLIP-FLOP: IMPLEMENTATION WITH NAND GATES



Q is the output of the S gate !

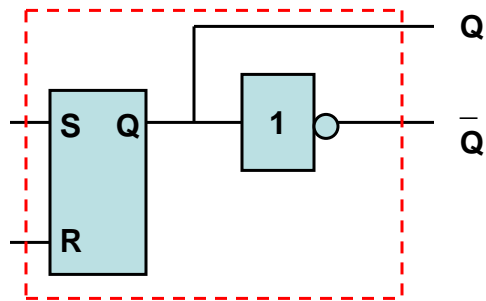
S	R	Q	Q̄
0	0	Q ₋₁	Q̄ ₋₁
0	1	0	1
1	0	1	0
1	1	(1)	(1) (not allowed)

$$Q = \bar{S} \bar{Q}$$

$$Q = \bar{R} Q$$

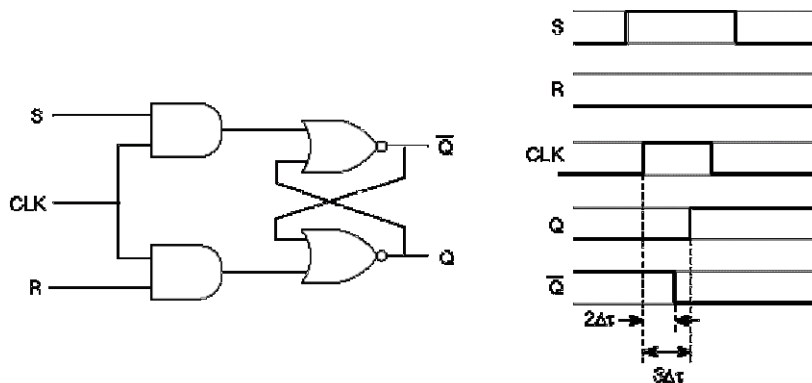
SR FLIP-FLOP

The problem of logically undefined state ($S = R = 1$) can be handled by using an additional inverter to generate \bar{Q} from Q (for NAND gate realization):



For the excitation $SR = 1$ the output will be $Q = 1$, i.e. the S input has the priority.

CLOCKED S-R FLIP-FLOP

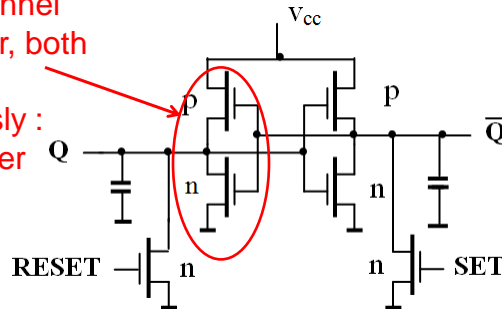


The clock signal, CLK, turns on the inputs to the flip-flop.

$$Q^{n+1} = S \bar{G} + \bar{R} \bar{G} Q^n$$

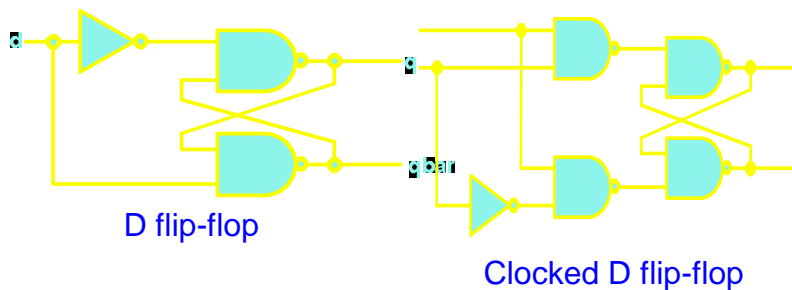
CMOS STATIC RS FLIP-FLOP

N- and p-channel
MOSFET pair, both
gates driven
simultaneously :
CMOS inverter



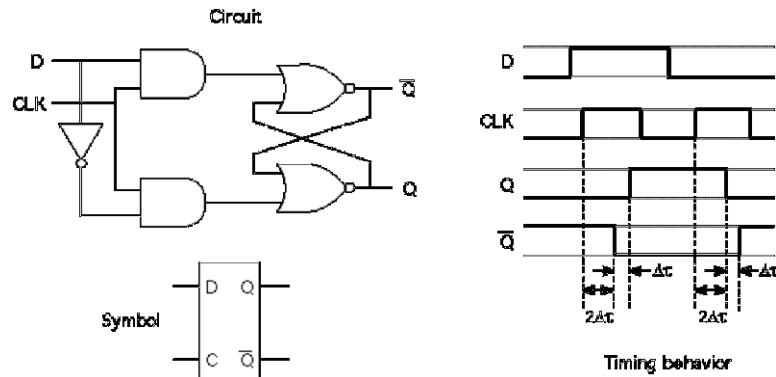
Set and Reset: with pull-down transistors. Flipping occurs by "brute force", e.g. by activating RESET, C is discharged through T1 while the upper pMOS simultaneously pulls it up by charging. Using a sufficiently large current T1, the circuit will flip, however the power dissipation and the time delay are relatively large.

D FLIP-FLOP: CHARACTERISTICS



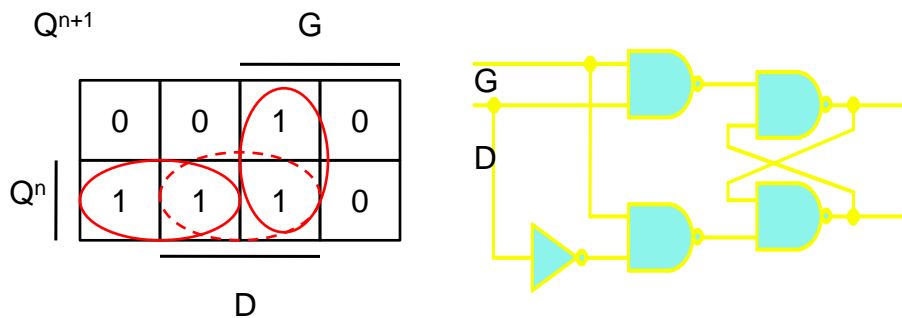
Avoids the instability of the RS flip-flop
Retains its last input value
Formally known as a "Delay" flip-flop ("Data" flip-flop)
May become unstable if transitions are too close together
Is generally implemented as a special circuit, *not* as pictured here.

THE CLOCKED D (DATA) FLIP-FLOP



The clocked D flip-flop, sometimes called a latch, has a potential problem: If D changes while the clock is high, the output will also change. The Master-Slave flip-flop solves this problem.

GATED D FLIP-FLOP



$$Q^{n+1} = D G + \bar{G} Q^n + D Q^n$$

The third term is necessary for the elimination of (static) race hazards.

In each column there is at least one stable state, so the D FF can be operated asynchronously too.

EDGE-TRIGGERED FLIP-FLOP

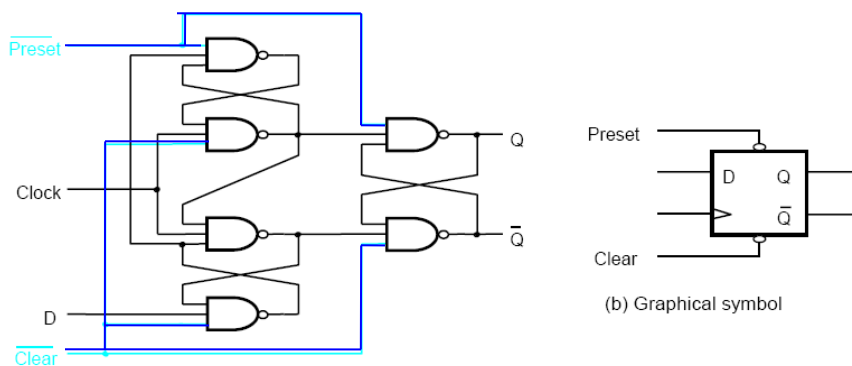
The inputs to the latches/FFs we have seen so far are controlled by the level of the clock: level-sensitive FFs.

It is possible to construct FFs that are edge triggered:

The output changes only at the point of time when the clock changes from one to the other.

Circuits are called edge-triggered.

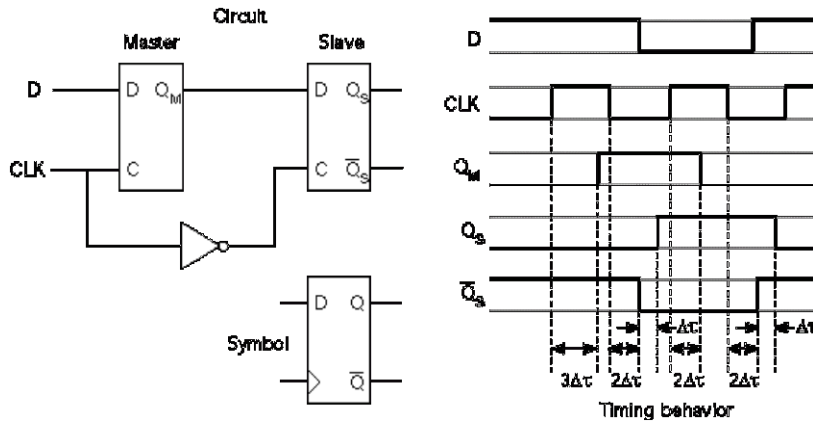
EDGE-TRIGGERED D FLIP-FLOP



Logic structure of edge-triggered D flip-flop (logic diagram of type 7474).

Auxiliary circuitry: asynchronous CLEAR and PRESET

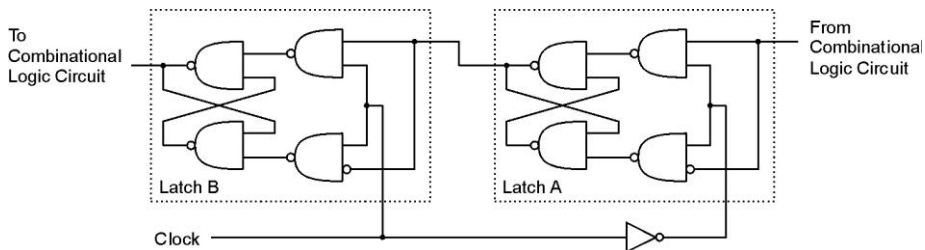
THE MASTER-SLAVE FLIP-FLOP



The rising edge of the clock clocks new data into the Master, while the Slave holds previous data. The falling edge clocks the new Master data into the Slave.

MASTER-SLAVE FLIP-FLOP

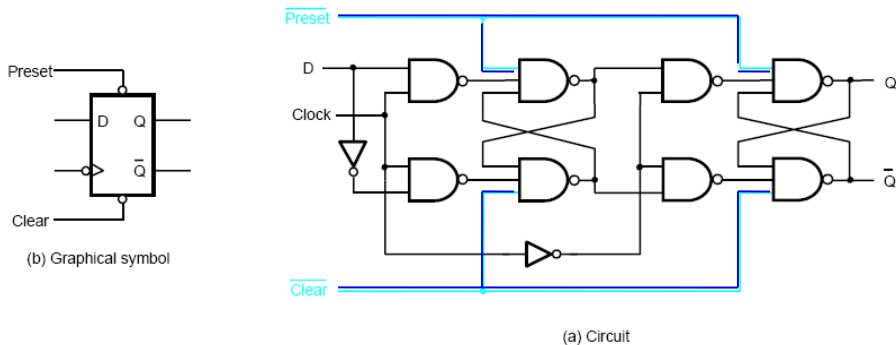
- A pair of gated D-latches, to isolate *next* state from *current* state.



During 1st phase (clock=1), previously-computed state becomes *current* state and is sent to the logic circuit.

During 2nd phase (clock=0), *next* state, computed by logic circuit, is stored in Latch A.

MASTER-SLAVE D FLIP-FLOP: LOGIC DIAGRAM

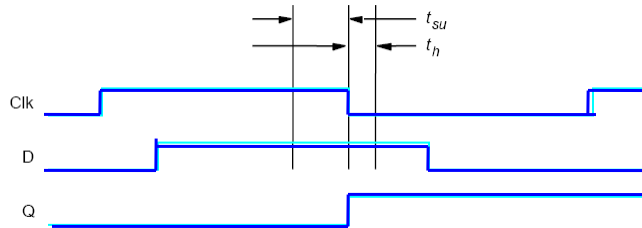


Auxiliary circuitry: asynchronous CLEAR and PRESET

FLIP-FLOP TIMING PARAMETERS

Certain timing parameters would be listed in the specification sheet of a flip-flop. Some of these parameters, are specific to the logic family to which the flip-flop belongs. There are some parameters that have different values for different flip-flops belonging to the same broad logic family. It is therefore important that one considers these timing parameters before using a certain flip-flop in a given application. Some of the important ones are *set-up* and *hold times*, *propagation delay*, *clock pulse HIGH* and *LOW times*, *asynchronous input active pulse width*, *clock transition time* and *maximum clock frequency*.

SETUP AND HOLD TIMES



Cannot ignore effect of propagation delay.

Need to worry about critical timing region.

Setup time: minimum time that the signal D must be stable prior to the edge of the clock.

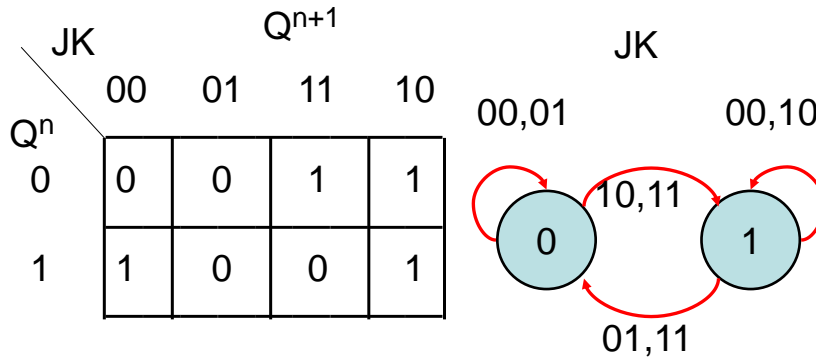
Hold time: minimum time that the signal must be stable after the edge of the clock.

JK FLIP-FLOP

The JK flip-flop augments the behaviour of the SR flip-flop by interpreting the $S = R = 1$ conditions as a "flip" ("toggle") command:

J	K	Q_{next}	Comment
0	0	Q_{prev}	hold state
0	1	0	reset
1	0	1	set
1	1	$\overline{Q_{prev}}$	toggle

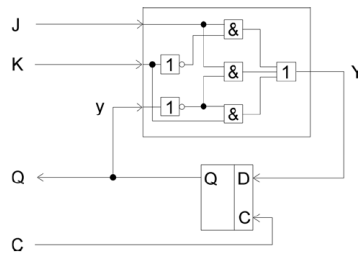
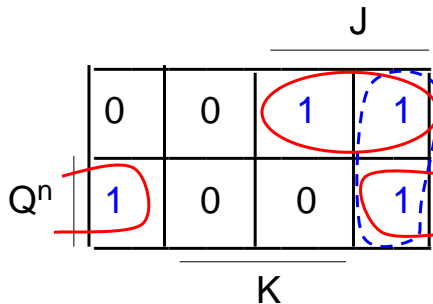
J-K FLIP-FLOP: STATE TRANSITION TABLE AND DIAGRAM



There is no stable state in the $J=K=1$ column, therefore the JK flip-flop can only be realized on the form of synchronous sequential (i.e. clocked) circuit.

J-K FLIP-FLOP: CHARACTERISTIC EQUATION

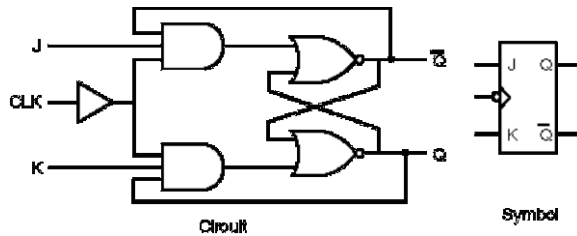
Implementation „in principle”



The third term in the equation is necessary for the elimination of race hazards

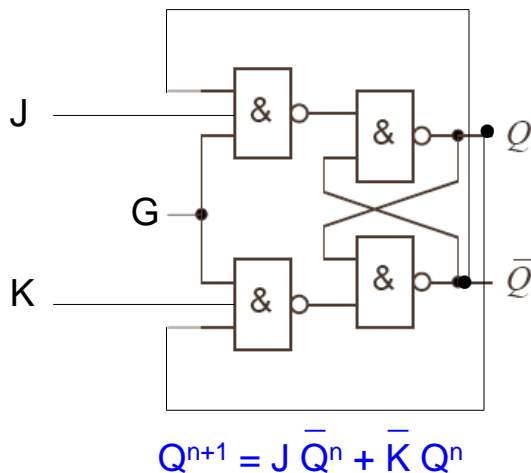
$$Q^{n+1} = J \bar{Q}^n + \bar{K} Q^n + J K$$

THE BASIC J-K FLIP-FLOP

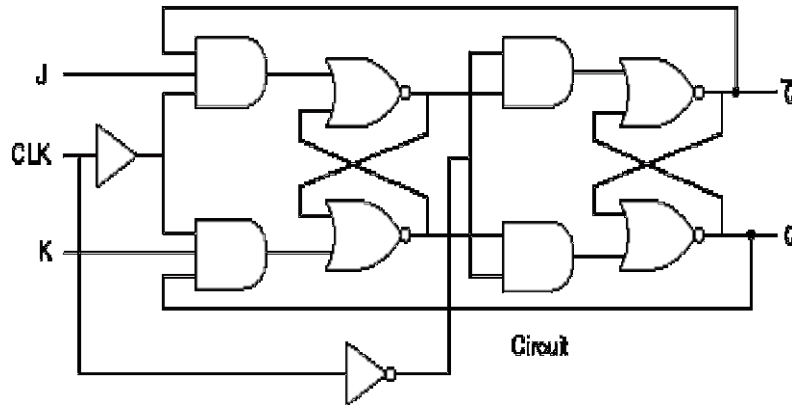


- The J-K flip-flop eliminates the S=R=1 problem of the S-R flip-flop, because Q enables J while Q' disables K, and vice-versa.
- However there is still a problem. If J goes momentarily to 1 and then back to 0 while the flip-flop is active and in the reset, the flip-flop will "catch" the 1.
- This is referred to as "1's catching."
- The J-K Master-Slave flip-flop solves this problem.

GATED/CLOCKED JK FLIP-FLOP



THE MASTER-SLAVE J-K FLIP-FLOP



T-FLIP-FLOP

The output of a toggle flip-flop, also called a T flip-flop, changes state every time it is triggered at its T input, called the toggle input.

T flip-flops do not really exist (!), constructed from JK or D FFs.

Usually best choice for implementing counters.

To create a T-FF using a D flip-flop.

Add a feedback connection that makes the input signal D equal either the value of Q or Q' under the control of the signal T.

CHARACTERISTIC EQUATIONS OF FLIP-FLOPS: A SUMMARY

RS		$Q^{n+1} = S + \bar{R} Q^n$
JK		$Q^{n+1} = J \bar{Q}^n + \bar{K} Q^n + J \bar{K}$
T		$Q^{n+1} = \bar{T} Q^n + T \bar{Q}^n = T \oplus Q^n$
D		$Q^{n+1} = D^n$
D-G		$Q^{n+1} = D G + \bar{G} Q^n + D \bar{Q}^n$

Note: The third terms in the equation of JK and D-G flip-flops serve for the elimination of race hazards

EXCITATION TABLES OF FLIP-FLOPS

Q ⁿ	Q ⁿ⁺¹	R	S	J	K	D	T
0	0	x	0	0	X	0	0
0	1	0	1	1	X	1	1
1	0	1	0	X	1	0	1
1	1	0	X	X	0	1	0

The excitation table lists the required inputs for a given change of state, i.e. the input conditions that will cause the transition from a given present state to the next state. The excitation table is required and is used in the design process.

SUMMARY OF FLIP-FLOP TYPES

FLIP-FLOP NAME	FLIP-FLOP SYMBOL	CHARACTERISTIC TABLE	CHARACTERISTIC EQUATION	EXCITATION TABLE																																				
SR		<table border="1"> <thead> <tr> <th>S</th> <th>R</th> <th>Q_{next}</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>Q</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>?</td> </tr> </tbody> </table>	S	R	Q_{next}	0	0	Q	0	1	0	1	0	1	1	1	?	$Q_{next} = S + R'Q$ $SR = 0$	<table border="1"> <thead> <tr> <th>Q</th> <th>Q_{next}</th> <th>S</th> <th>R</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> <td>X</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>X</td> <td>0</td> </tr> </tbody> </table>	Q	Q_{next}	S	R	0	0	0	X	0	1	1	0	1	0	0	1	1	1	X	0	S=R=1 not allowed
S	R	Q_{next}																																						
0	0	Q																																						
0	1	0																																						
1	0	1																																						
1	1	?																																						
Q	Q_{next}	S	R																																					
0	0	0	X																																					
0	1	1	0																																					
1	0	0	1																																					
1	1	X	0																																					
JK		<table border="1"> <thead> <tr> <th>J</th> <th>K</th> <th>Q_{next}</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>Q</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>Q'</td> </tr> </tbody> </table>	J	K	Q_{next}	0	0	Q	0	1	0	1	0	1	1	1	Q'	$Q_{next} = JQ' + K'Q$	<table border="1"> <thead> <tr> <th>Q</th> <th>Q_{next}</th> <th>J</th> <th>K</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> <td>X</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> <td>X</td> </tr> <tr> <td>1</td> <td>0</td> <td>X</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>X</td> <td>0</td> </tr> </tbody> </table>	Q	Q_{next}	J	K	0	0	0	X	0	1	1	X	1	0	X	1	1	1	X	0	Most versatile type
J	K	Q_{next}																																						
0	0	Q																																						
0	1	0																																						
1	0	1																																						
1	1	Q'																																						
Q	Q_{next}	J	K																																					
0	0	0	X																																					
0	1	1	X																																					
1	0	X	1																																					
1	1	X	0																																					
D		<table border="1"> <thead> <tr> <th>D</th> <th>Q_{next}</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> </tr> <tr> <td>1</td> <td>1</td> </tr> </tbody> </table>	D	Q_{next}	0	0	1	1	$Q_{next} = D$	<table border="1"> <thead> <tr> <th>Q</th> <th>Q_{next}</th> <th>D</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <td>1</td> <td>1</td> <td>1</td> </tr> </tbody> </table>	Q	Q_{next}	D	0	0	0	0	1	1	1	0	0	1	1	1	Most simple Gated (DG) Copies input to output														
D	Q_{next}																																							
0	0																																							
1	1																																							
Q	Q_{next}	D																																						
0	0	0																																						
0	1	1																																						
1	0	0																																						
1	1	1																																						
T		<table border="1"> <thead> <tr> <th>T</th> <th>Q_{next}</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>Q</td> </tr> <tr> <td>1</td> <td>Q'</td> </tr> </tbody> </table>	T	Q_{next}	0	Q	1	Q'	$Q_{next} = TQ' + T'Q$	<table border="1"> <thead> <tr> <th>Q</th> <th>Q_{next}</th> <th>T</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>0</td> </tr> </tbody> </table>	Q	Q_{next}	T	0	0	0	0	1	1	1	0	1	1	1	0	Complements output if activated														
T	Q_{next}																																							
0	Q																																							
1	Q'																																							
Q	Q_{next}	T																																						
0	0	0																																						
0	1	1																																						
1	0	1																																						
1	1	0																																						

IMPLEMENTATION OF FLIP-FLOPS: SOME PRACTICAL ASPECTS

- In the popular CMOS and TTL logic families T flip-flop is not available. It should be build on the basis of an other type of flip-flop.
- TTL, CMOS: basically JK and D flip-flops.
- PLA, PLD: only D flip-flop (!), the JK flip-flop should be implemented by additional circuitry.
- RS flip-flop: in TTL it is based on NAND gates, in CMOS it is based on NOR gates.

APPLICATION OF FLIP-FLOPS: SOME PRACTICAL ASPECTS

- T flip-flops are well suited for straightforward binary counters.
But may yield worst gate and pin counts.
- No reason to choose RS over JK FFs: it is a proper subset of JK. RS FFs don't exist anyway.
Tend to yield best choice for packaged logic where gate count is the key.
- D FFs yield simplest design procedure. In many cases give the best pin count.
D storage devices are very transistor efficient in VLSI.
Best choice where area/pin count is the key.

REVISION QUESTIONS

1. What do you mean by sequential circuit? Explain with the help of a block diagram.
2. Give the comparison and explain the differences between combinational and sequential circuits.
3. Give the comparison and explain the differences between synchronous and asynchronous sequential circuits.
4. What is the difference in the operation of edge-triggered FFs and master slave FFs.

REVISION QUESTIONS

5. Justify name Toggle for T flip-flop giving truth table and waveforms.
6. Give the characteristic equation for each flip-flop.
7. Draw the state transition diagrams for SR, D, JK and T flip-flop.
8. Derive the excitation tables for SR, D, JK and T flip-flop.

REVISION QUESTIONS

9. Perform the following conversions:

- Convert SR flip-flop to D flip-flop.
- Convert SR flip-flop to JK flip-flop.
- Convert SR flip-flop to T flip-flop.
- Convert JK flip-flop to T flip-flop.
- Convert JK flip-flop to D flip-flop.
- Convert D flip-flop to T flip-flop.
- Convert T flip-flop to D flip-flop.
- Convert JK flip-flop to SR flip-flop.
- Convert D flip-flop to SR flip-flop.

PROBLEMS AND EXERCISES

1. In a complete state machine, all possible transitions between states of a finite state machine (FSM) should be specified. Your state machine has two inputs, A and B, and two states, S0 and S1. You are told that your FSM behaves as follows:

The FSM moves from S0 to S1 if and only if $A = 1$.

The FSM moves from S1 to S0 if and only if $A = 0$ and $B = 1$.

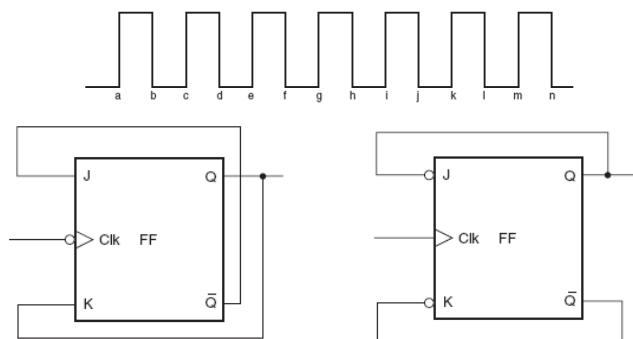
Draw the complete state transition diagram of your FSM.

2. Analyze the operation of the type 7474 edge triggered D flip-flop and give its full operational/truth table for asynchronous and synchronous control.

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PROBLEMS AND EXERCISES

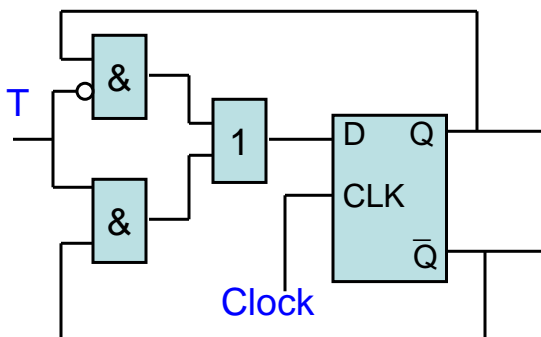
3. The 100 kHz square waveform shown below is applied to the clock input of the flip-flops shown in the figures. If the Q output is initially '0', draw the Q output waveform in the two cases. Also, determine the frequency of the Q output in the two cases.



END OF LECTURE ON FLIP-FLOPS

Supplement follows

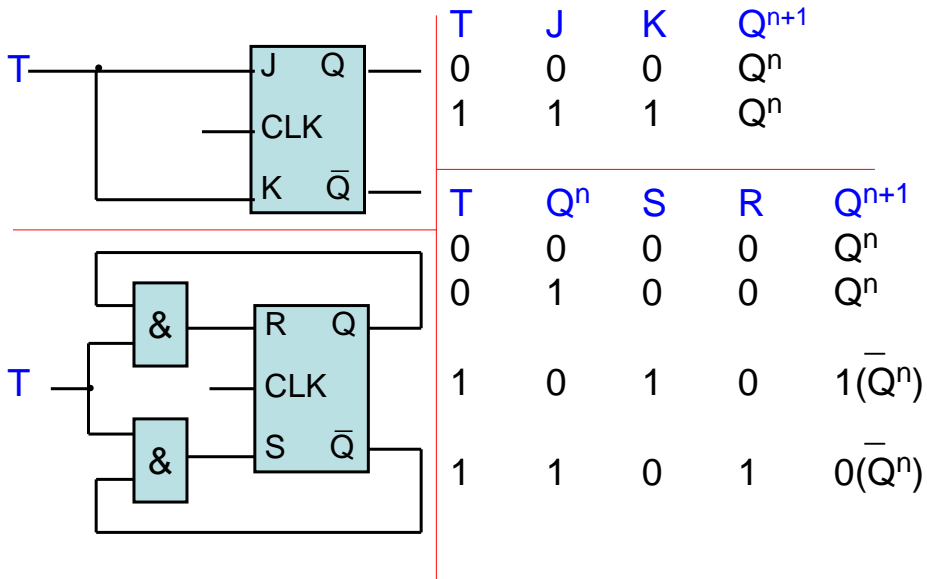
T FLIP-FLOP BUILT WITH A D FLIP-FLOP



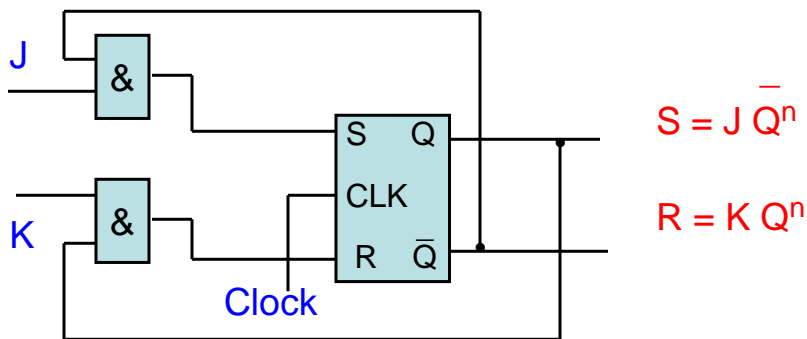
$$D = \bar{T} Q^n + T \bar{Q}^n$$

Note that T flip-flops are not available in the CMOS and TTL logic families. D flip-flops are available in PLDs.

VARIOUS IMPLEMENTATIONS OF A T FLIP-FLOP



JK FLIP-FLOP BUILT WITH RS FLIP-FLOP



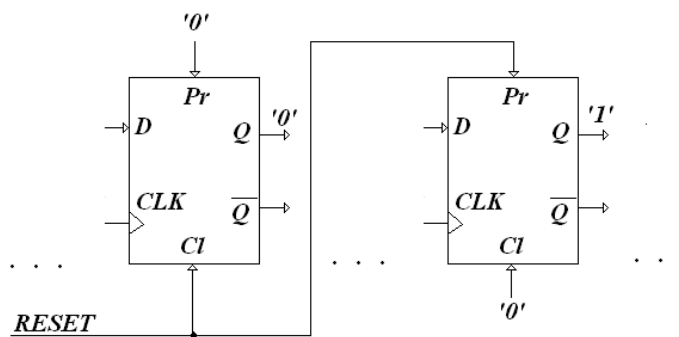
The feedback ensures that the not allowed $R=S=1$ condition can not occur.

PRACTICAL ASPECTS: SETTING INITIAL STATES

If in designing a synchronous sequential circuit, the encoding selected begins with full zeros (e.g. a simple counter), the auxiliary CLEAR and PRESET can be used. The PRESET is connected to 0 (zero), and to the CLEAR input the external R (RESET) signal is connected.

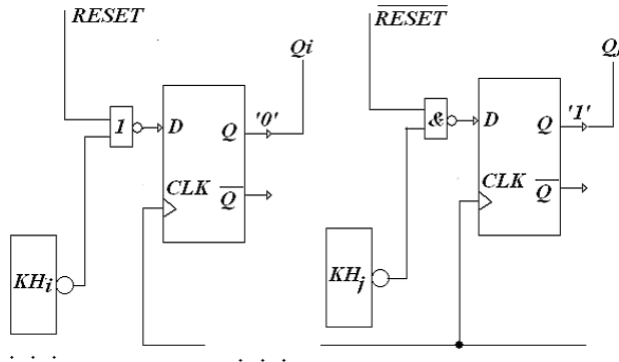
This can be generalized to any initial code (e.g. counter working in Excess-3 code) .

PRACTICAL ASPECTS: SETTING INITIAL STATES



Flip-flops with initial state 0 are activated through CLEAR, and those with initial state 1 are activated through PRESET.

PRACTICAL ASPECTS: SETTING INITIAL STATES



The initial state can also be established by using appropriate networks fitted into the combinational networks connected to the control inputs of the flip-flops.

PRACTICAL ASPECTS: SETTING INITIAL STATES

D_i	RESET	D_i'
0	0	0
0	1	0
1	0	1
1	1	0

$$D_i' = \overline{D \text{ RESET}}$$

$$= \overline{\overline{D} + \text{RESET}}$$

Left: initial state 0

D_j	RESET	D_j'
0	0	0
0	1	1
1	0	1
1	1	1

$$D_j' = \overline{\overline{D} \text{ RESET}}$$

right: initial state 1

SUMMARY OF SOME ASPECTS OF FLIP-FLOPS

Development of D flip-flop

Level-sensitive is used in custom ICs

Edge-triggered used in programmable logic devices

Good choice for data storage register

Historically JK flip-flop was popular but now never used

Similar to RS but with 11 used to toggle output

Good in days of TTL/SSI (more complex input function)

Not a good choice for PALs/PLAs as it requires two inputs

Can always be implemented using D flip-flops

Preset and clear inputs are highly desirable on flip-flops

Used at start-up or to reset systems to a known state

SUMMARY OF SOME ASPECTS OF FLIP-FLOPS

RS clocked latch:

Used as storage element in narrow width clocked systems

Its use is not recommended!

However fundamental building block of other flip-flop types

JK flip-flop:

Versatile building block

Can be used to implement D and T flip-flops

Usually requires least amount of logic to implement $f(I_n, Q)$

But has two inputs with increase wiring complexity

D flip-flops:

Minimizes wires, much preferred in VLSI technologies

Simplest design technique

Best choice for storage registers

T flip-flops:

Don't really exist, constructed from JK flip-flops

Usually best choice for implementing counters